



**COBEM**  
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# An Improved Ensemble Learning Model for Multi-Step Ahead Wind Power Generation Forecasting

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# Wind Power Data Set



- 15 Wind Turbines (WT);
- 2000kW rated power each;
- Rotor Diameter 90m;
- Rotor height 80m;
- August, 1<sup>st</sup> up to November, 20<sup>th</sup>, 2020;
- Installed Capacity 30000kW.

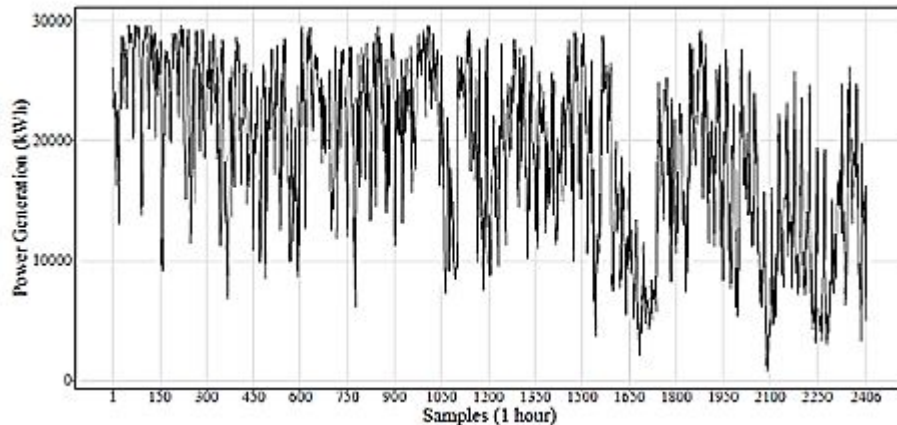


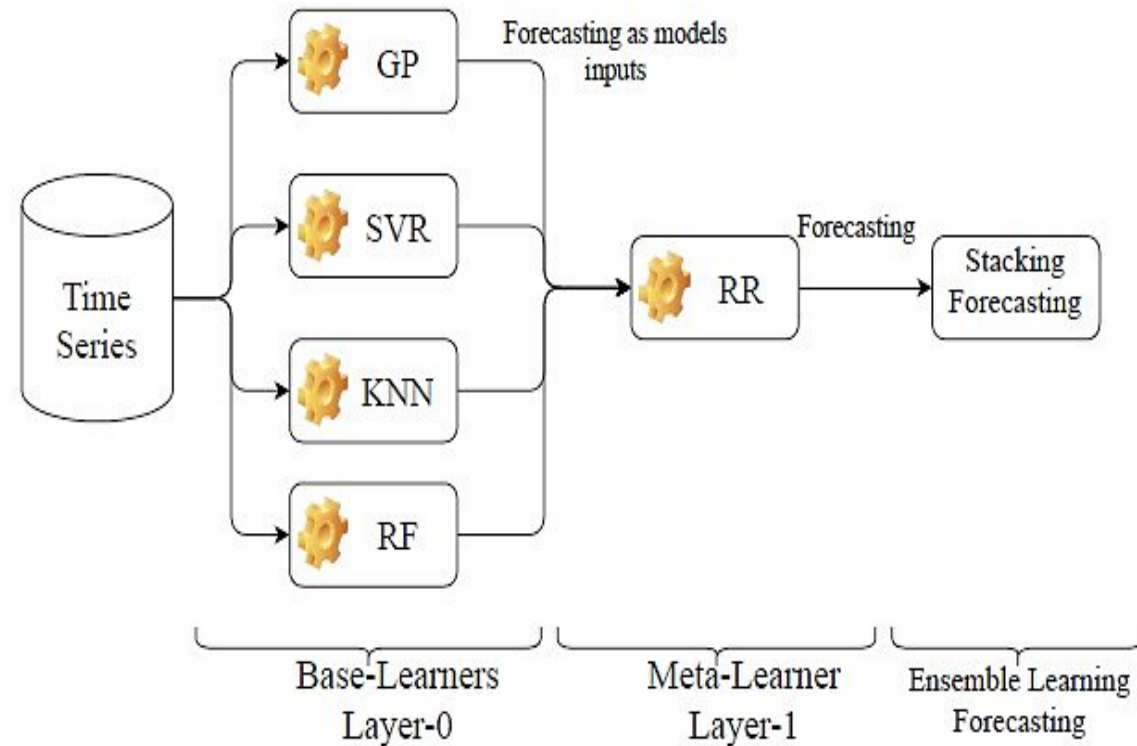
Table 1: Statistical indicators of wind power generation time series.

Dataset	Statistical Indicator					
	Minimum	Median	Mean	Maximum	Standard Deviation	# Samples
Whole	810.88	20093.76	19079.59	29627.22	6889.61	2406
Training	2108.69	22335.07	21100.39	29627.22	6000.78	1684
Test	810.88	14200.27	14366.25	29146.23	6518.65	722

# Proposed Method

## Stacking Learning Ensemble

- Base Learners Layer-0:
  - Gaussian process (GP);
  - Support Vector Regression with linear kernel (SVR);
  - k-Nearest Neighbor (kNN); and
  - Random Forests (RF).
- Meta Learner Layer-1
  - Ridge Regression (RR)
- Forecasting Horizon
  - 1 up to 12 hours-ahead
- Metrics
  - Root Mean Squared Error (RMSE);
  - Normalized RMSE (nRMSE);
  - Mean Absolute Error (MAE); and
  - Theil's U Index (UT)





# Results and Conclusion

Table 2: Performance measures of compared models for wind power generation forecasting.

Forecasting Horizon	Criteria	Stack	Stack + 10 Bootstraps			Stack + 30 Bootstraps			Stack + 50 Bootstraps			Stack + 100 Bootstraps		
		Original	Average	Median	Average	Median	Average	Median	Average	Median	Average	Median	Average	Median
1	RMSE	<b>2828.28</b>	3263.56	3269.56	3282.41	3281.12	3249.62	3247.45	3234.27	3230.37				
	nRMSE	<b>19.69%</b>	22.72%	22.76%	22.85%	22.84%	22.62%	22.60%	22.51%	22.49%				
	MAE	<b>2143.38</b>	2658.33	2654.99	2666.80	2667.84	2650.65	2645.63	2624.77	2616.27				
	UT	<b>0.1757</b>	0.2088	0.2082	0.2104	0.2096	0.2084	0.2073	0.2073	0.2061				
2	RMSE	3619.77	3627.37	3633.27	3619.22	3601.62	3615.68	3614.11	3589.65	<b>3587.29</b>				
	nRMSE	25.20%	25.25%	25.29%	25.19%	25.07%	25.17%	25.16%	24.99%	<b>24.97%</b>				
	MAE	<b>2794.92</b>	2948.79	2953.97	2950.43	2935.89	2953.71	2949.19	2927.37	2919.55				
	UT	<b>0.2228</b>	0.2309	0.2305	0.2309	0.2293	0.2308	0.2296	0.2290	0.2279				
3	RMSE	3965.14	3843.91	3831.81	3847.81	3832.02	3851.32	3850.22	3819.64	<b>3816.36</b>				
	nRMSE	27.60%	26.76%	26.67%	26.78%	26.67%	26.81%	26.80%	26.59%	<b>26.56%</b>				
	MAE	<b>3106.56</b>	3150.51	3149.94	3133.94	3112.65	3156.10	3149.30	3121.94	3116.57				
	UT	0.2442	0.2446	0.2431	0.2457	0.2443	0.2456	0.2448	0.2436	<b>0.2426</b>				
4	RMSE	4299.16	4038.70	4020.25	4036.19	4021.39	4031.32	4024.26	4017.22	<b>4015.05</b>				
	nRMSE	29.93%	28.11%	27.98%	28.09%	27.99%	28.06%	28.01%	27.96%	<b>27.95%</b>				
	MAE	3439.89	3307.92	3306.61	3281.34	<b>3268.64</b>	3303.48	3291.35	3287.81	3285.06				
	UT	0.2655	0.2571	0.2558	0.2574	0.2561	0.2576	0.2559	0.2563	<b>0.2554</b>				
5	RMSE	4745.92	4311.46	4298.85	4253.71	<b>4237.61</b>	4262.42	4267.57	4275.31	4279.48				
	nRMSE	33.04%	30.01%	29.92%	29.61%	<b>29.50%</b>	29.67%	29.71%	29.76%	29.79%				
	MAE	3753.23	3563.41	3553.66	3485.50	<b>3472.47</b>	3524.86	3523.52	3523.55	3519.53				
	UT	0.2857	0.2705	0.2694	0.2679	<b>0.2666</b>	0.2676	0.2672	0.2679	0.2673				
6	RMSE	4980.08	4431.71	4422.91	4407.80	4396.45	4405.82	4414.56	<b>4380.39</b>	4381.94				
	nRMSE	34.67%	30.85%	30.79%	30.68%	30.60%	30.67%	30.73%	<b>30.49%</b>	30.50%				
	MAE	4068.44	3629.18	3630.24	3600.70	3583.04	3613.53	3615.79	3588.88	<b>3580.12</b>				
	UT	0.3048	0.2845	0.2830	0.2844	0.2834	0.2834	0.2831	0.2813	<b>0.2807</b>				

Table 3: Performance measures of compared models for wind power generation forecasting.

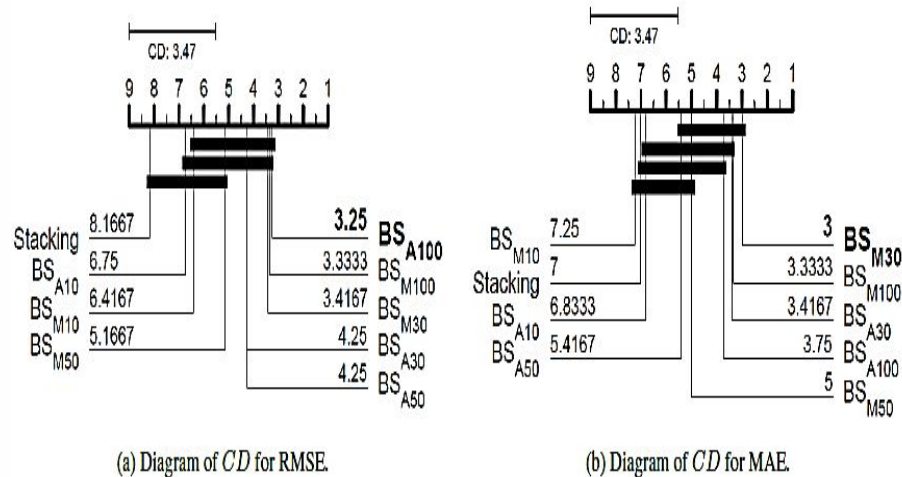
Forecasting Horizon	Criteria	Stack	Stack + 10 Bootstraps			Stack + 30 Bootstraps			Stack + 50 Bootstraps			Stack + 100 Bootstraps		
		Original	Average	Median	Average	Median	Average	Median	Average	Median	Average	Median	Average	Median
7	RMSE	5270.26	4617.50	4628.60	<b>4533.12</b>	4542.79	4580.91	4594.23	4581.73	4559.18				
	nRMSE	36.69%	32.14%	32.22%	<b>31.55%</b>	31.62%	31.89%	31.98%	31.89%	31.74%				
	MAE	4330.83	3815.19	3820.15	<b>3715.38</b>	3724.50	3770.34	3772.40	3756.30	3738.98				
	UT	0.3090	0.2888	0.2884	<b>0.2827</b>	0.2831	0.2856	0.2858	0.2855	0.2836				
8	RMSE	5642.22	4944.71	4947.58	4886.27	4876.31	4885.22	4893.83	<b>4871.47</b>	4881.43				
	nRMSE	39.27%	34.42%	34.44%	34.01%	33.94%	34.00%	34.06%	<b>33.91%</b>	33.98%				
	MAE	4623.75	4078.54	4088.49	<b>3976.37</b>	3977.77	4012.46	4013.49	4001.76	4010.42				
	UT	0.3342	0.3080	0.3072	0.3073	0.3062	0.3060	0.3054	0.3049	<b>0.3046</b>				
9	RMSE	5630.98	5013.70	5027.65	<b>4976.59</b>	4989.36	5008.38	5020.91	5021.83	5018.92				
	nRMSE	39.20%	34.90%	35.00%	<b>34.64%</b>	34.73%	34.86%	34.95%	34.96%	34.94%				
	MAE	4572.41	4131.90	4157.31	<b>4102.29</b>	4107.94	4132.87	4129.94	4139.83	4131.96				
	UT	0.3334	0.3106	0.3105	0.3103	<b>0.3101</b>	0.3110	0.3110	0.3122	0.3111				
10	RMSE	5672.43	5088.86	5110.29	<b>5022.55</b>	5029.13	5042.02	5058.06	5033.94	5038.41				
	nRMSE	39.48%	35.42%	35.57%	<b>34.96%</b>	35.01%	35.10%	35.21%	35.04%	35.07%				
	MAE	4565.26	4213.07	4237.94	<b>4134.96</b>	4142.64	4171.57	4183.56	4159.95	4162.16				
	UT	0.3336	0.3136	0.3145	0.3116	0.3116	0.3105	0.3105	0.3106	<b>0.3100</b>				
11	RMSE	5851.22	5206.03	5193.34	<b>5132.27</b>	5137.94	5146.48	5162.33	5150.96	5167.22				
	nRMSE	40.73%	36.24%	36.15%	<b>35.72%</b>	35.76%	35.82%	35.93%	35.85%	35.97%				
	MAE	4703.26	4275.71	4266.79	<b>4194.70</b>	4206.75	4227.47	4238.53	4217.68	4229.88				
	UT	0.3352	0.3201	0.3175	0.3177	0.3172	0.3158	<b>0.3158</b>	0.3166	0.3166				
12	RMSE	6004.80	5419.08	5385.52	5469.57	5473.68	<b>5380.41</b>	5404.83	5410.85	5424.00				
	nRMSE	41.80%	37.72%	37.49%	38.07%	38.10%	<b>37.45%</b>	37.62%	37.66%	37.76%				
	MAE	4968.50	4470.93	4451.70	4486.47	4484.83	<b>4413.89</b>	4436.98	4446.02	4451.88				
	UT	0.3569	0.3424	<b>0.3397</b>	0.3476	0.3480	0.3410	0.3413	0.3424	0.3423				

Table 4: Frequency distribution of best results according to the compared methods.

Aggregation	Stacking	Stacking + 10 Bootstraps	Stacking + 30 Bootstraps	Stacking + 50 Bootstraps	Stacking + 100 Bootstraps	Total
-	14.58%	-	-	-	-	14.58%
Average	-	0.00%	29.17%	6.25%	8.33%	43.75%
Median	-	2.08%	12.50%	2.08%	25%	41.67%
Total	14.58%	2.08%	41.67%	8.33%	33.33%	100.00%



# Results and Conclusion



- Accuracy and Forecasting Horizon:

- In 85.42% of all comparisons, the stacking combined with bagging ensemble has better accuracy than the stacking ensemble learning model;
- For one-hour-ahead forecasting, the stacking ensemble learning achieves forecasting errors lower than the combination of stacking with bagging ensemble approach according to all performance criteria;
- These two approaches have competitive results concerning the forecasting horizons of two and three-hours-ahead;

- Bootstrapping Samples

- Better forecasting results regarding the performance measures are achieved when 30 bootstrap samples are considered in the ensemble structure, followed by 100, 50, and 10;

- Aggregation strategy

- Similar accuracy



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